

# Vehicle Dynamics and Simulation

## Ride Dynamics

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# Lecture overview

- Excitation input
- Quarter car model
- Ride response
  - Active suspension
- Human perception

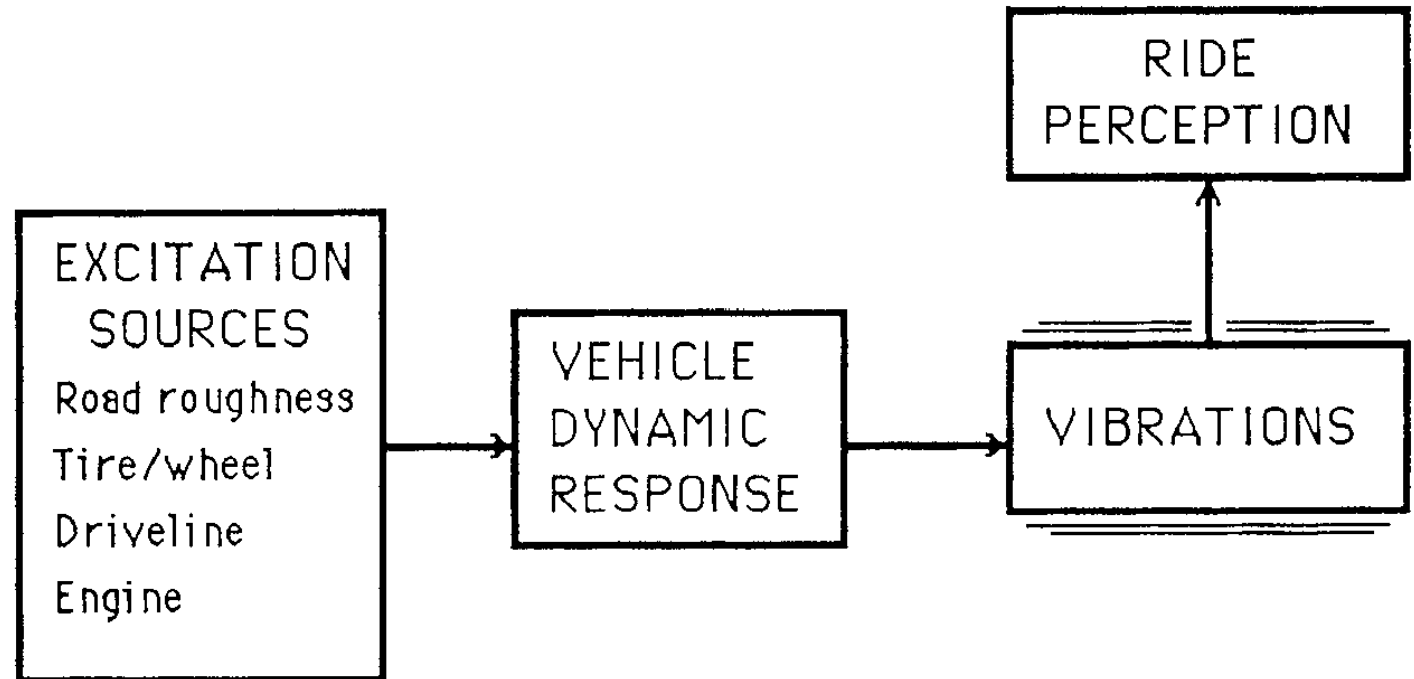


# The Ride System

- The Ride System

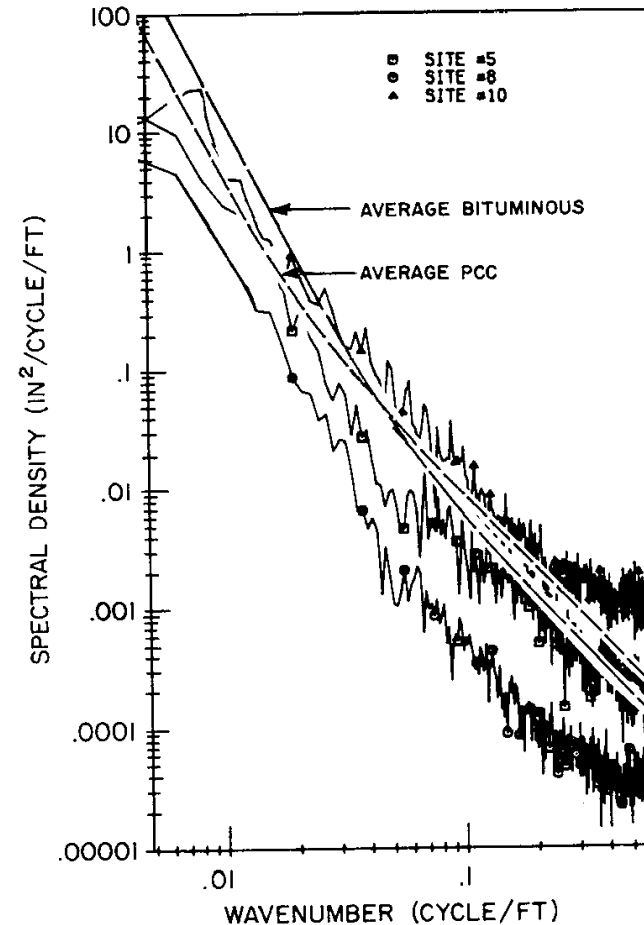
- Excitation
- Response
- Vibration
- Perception

- Analyses in time or frequency domains



# Excitation: Road Roughness

- The road surface is the most significant excitation source.



# Excitation: Road Roughness

- A model for generating excitation input
- Generator source: random sequence
- Described using;

$$G_Z(\nu) = G_O \left[ 1 + (\nu_o / \nu)^2 \right] / (2\pi\nu)^2 \quad [1]$$

where;

$G_Z(\nu)$  = PSD amplitude (feet<sup>2</sup>/cycle/foot)

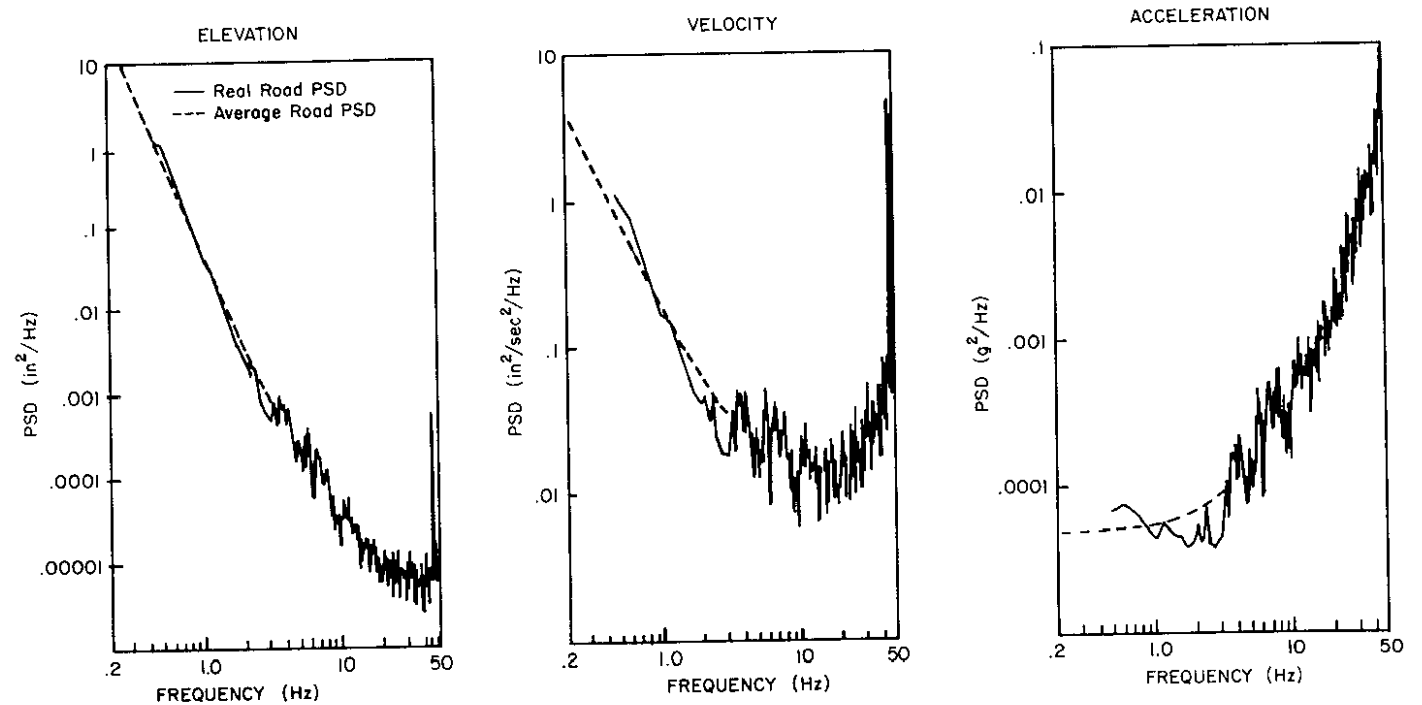
$\nu$  = Wavenumber (cycles/foot)

$G_O$  = Roughness magnitude parameter (1.25x10<sup>5</sup> for rough roads, 1.25x10<sup>6</sup> for smooth)

$\nu_o$  = Cutoff wavenumber (0.02 cycles/foot for rough roads, 0.05 cycles/foot for smooth)

# Excitation: Road Roughness

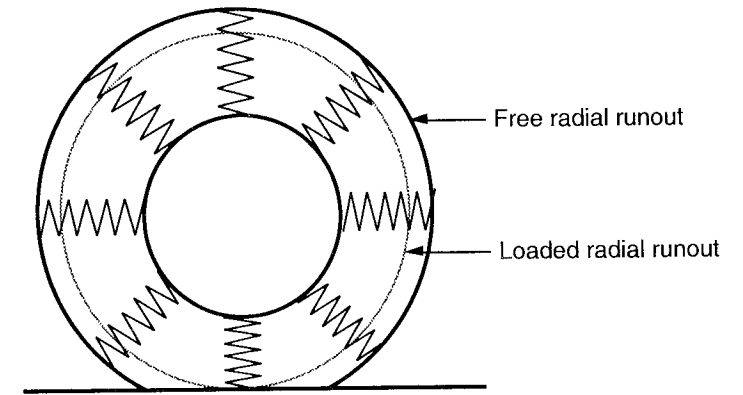
- Simulated roads can be created using [1] or a random number sequence (coloured noise)
- Multiplying cycles/distance (cyc/ft, cyc/m) by vehicle speed gives frequency - > from which PSD can be plotted.



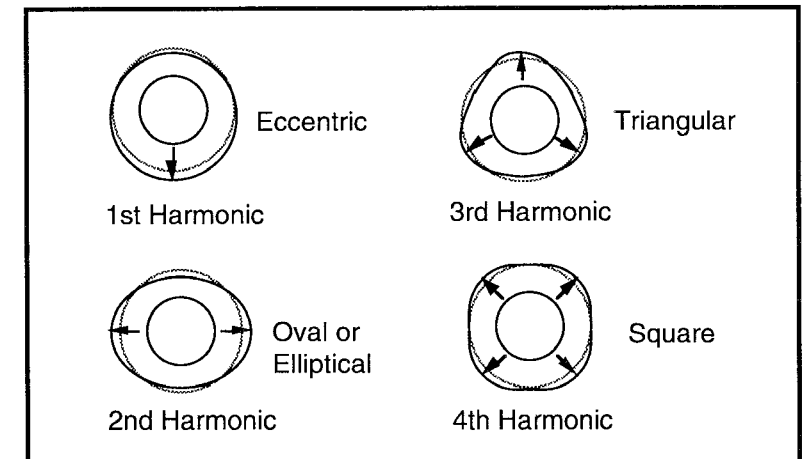
Frequency [cyc/s] = wave number [cyc/m] x speed [m/s]

# Excitation: Secondary Effects

- Secondary effects include vibration
  - Driveline
  - Engine
  - Wheel/tyre
- Typically, at higher frequency than primary excitation sources
- Runout occurs due to deformation of the tyre. Imperfections result in different harmonics i.e., mode shapes

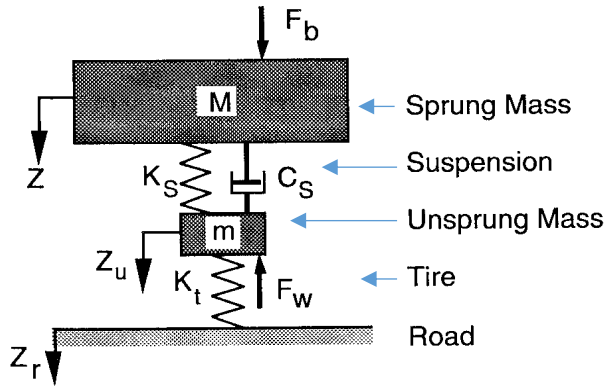


'Runout' due to tyre deformation



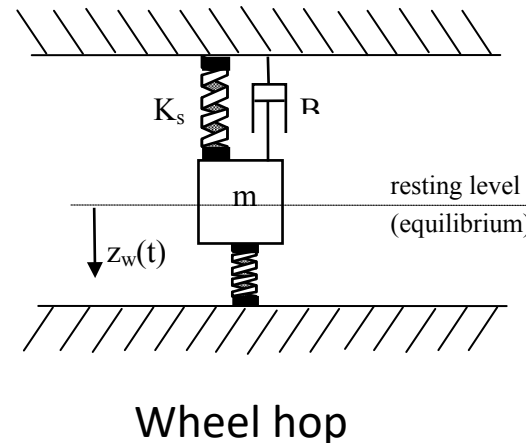
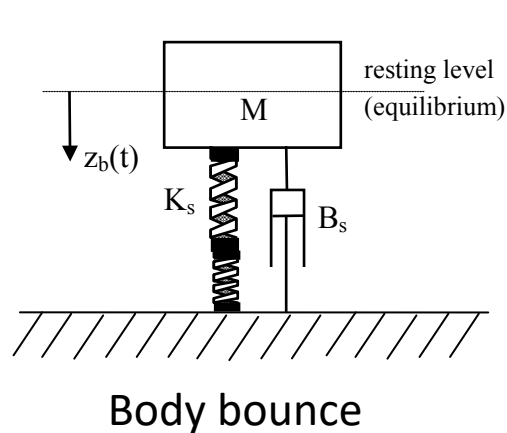
# The Quarter Car Model

- The simplest 'useful' representation of vertical ride dynamics



$M = 300\text{kg}$   
 $m = 30\text{kg}$   
 $K_s = 20000\text{ N/m}$   
 $K_t = 160000\text{ N/m}$   
 $C_s = 1500\text{ Ns/m}$  (also written as  $B_s$  below)

- More simple representations (for quick calcs) is possible considering different modes in isolation.





# The Quarter Car Model: Body bounce

- Considering body bounce (springs acting in series);

$$K_{bb} = \frac{K_s K_t}{K_s + K_t}$$

- The natural frequency,  $\omega_n$ ;

$$\omega_n = \sqrt{\frac{K_{bb}}{M}}$$

- The actual response is damped by the damping ratio,  $\zeta$  (typically 0.2 – 0.4)

$$\omega_d = \omega_n \sqrt{1 - \zeta^2} \quad \text{with} \quad \zeta = \frac{B_s}{\sqrt{4K_{bb}M}}$$

# The Quarter Car Model: Wheel hop

- For wheel hop;

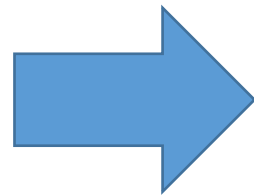
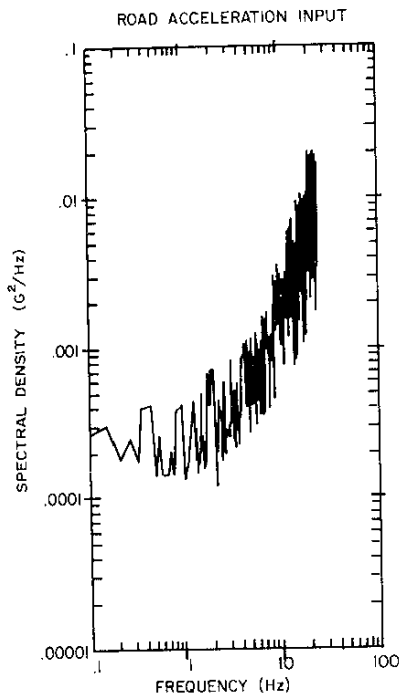
$$K_{wh} = K_s + K_t$$

- So that the natural frequency,  $\omega_n$

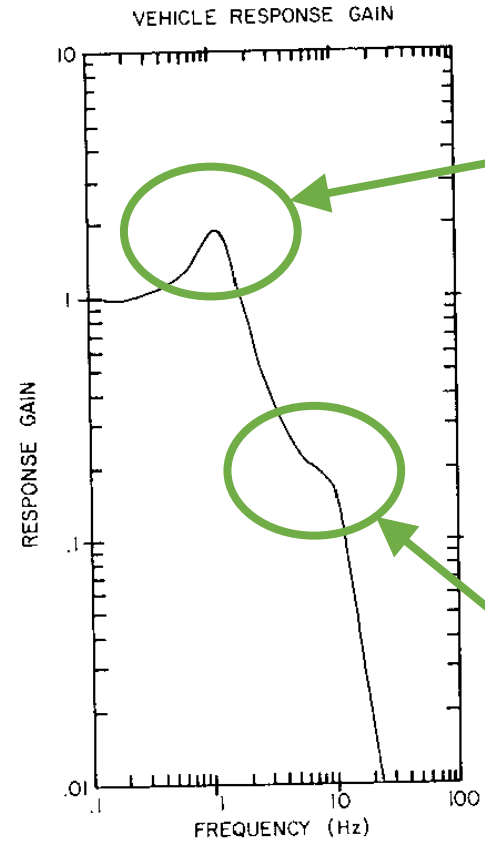
$$\omega_n = \sqrt{\frac{K_{wh}}{m}}$$

# Ride Response

Input: from road

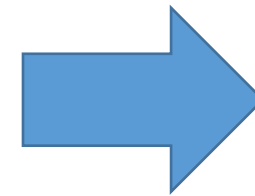


Modelled system

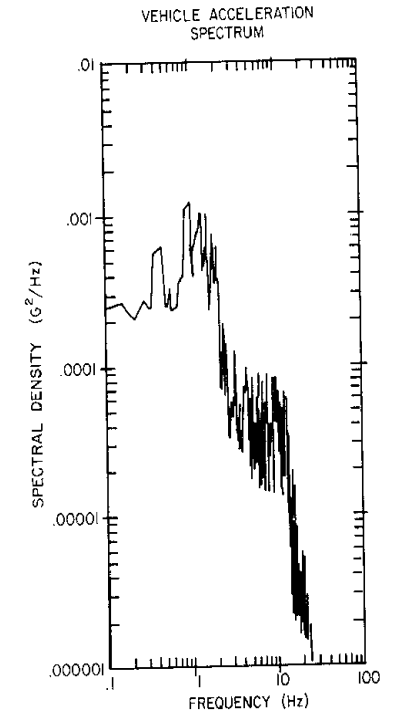


Body bounce

Wheel hop



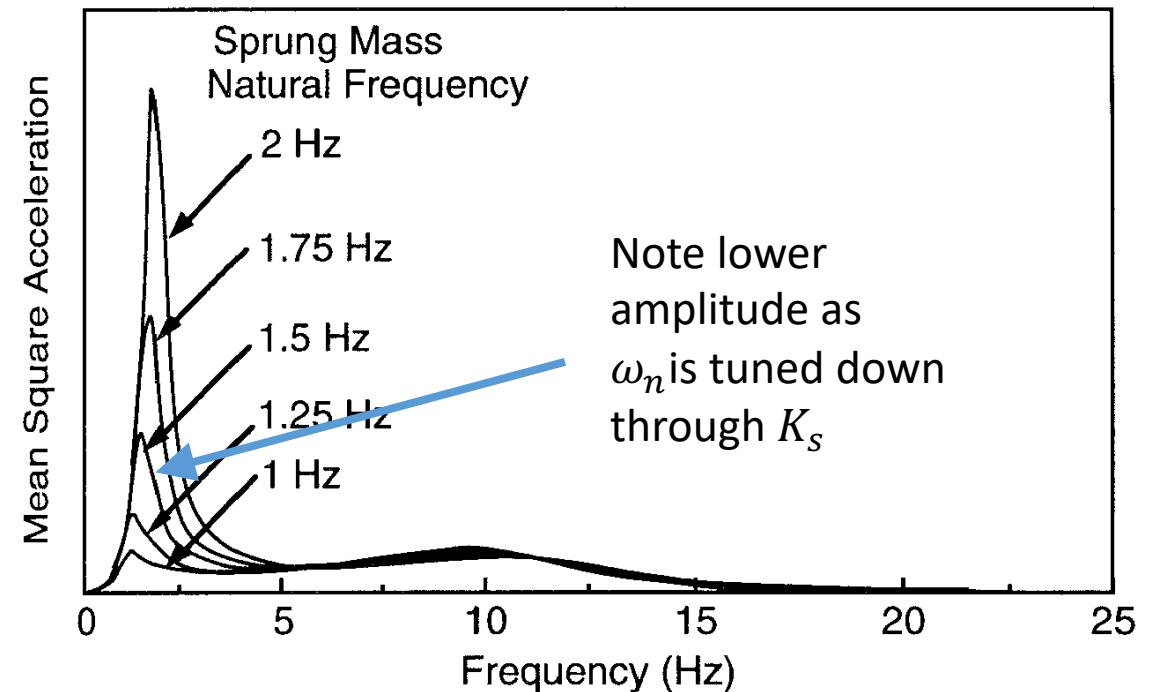
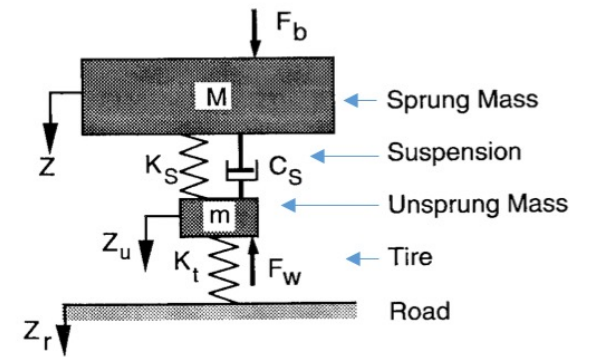
Output: suspension response



High frequency  
attenuation

# Ride Response

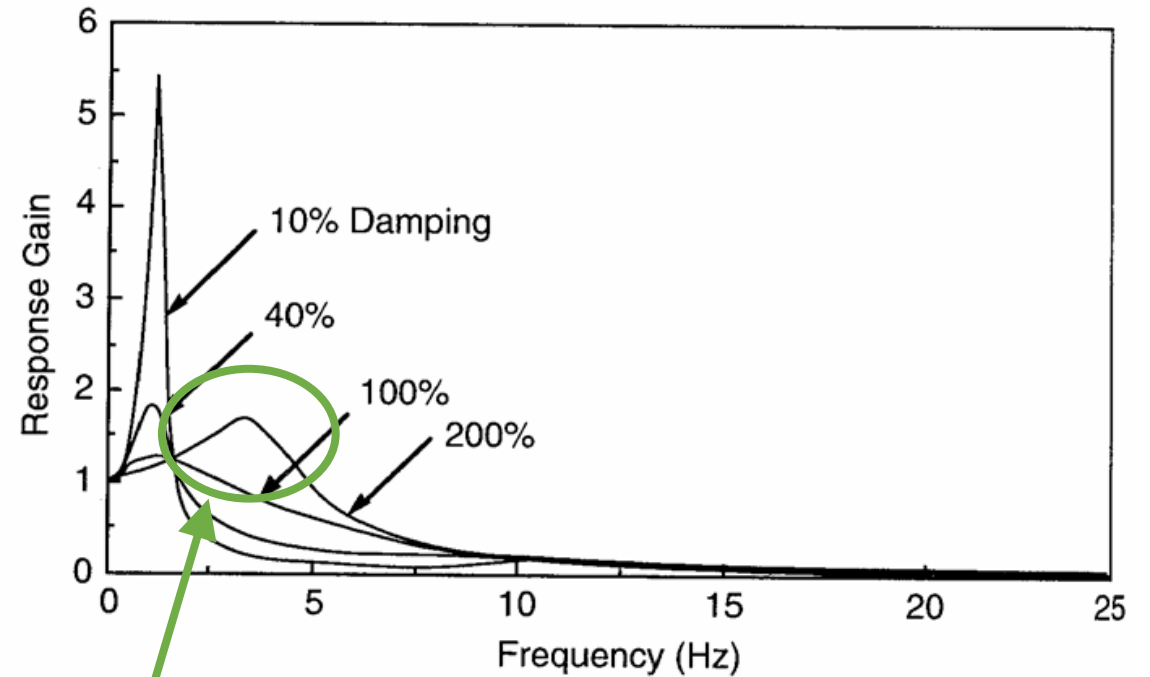
- $\omega_n$  of the sprung mass can be changed by changing stiffness,  $K_{bb}$ .
- $K_S$  and  $K_t$  act in series.  $K_t$  is significantly stiffer and therefore the response is dominated by  $K_S$ .
- Limited by;
  - Suspension travel
  - Handling performance
  - Nausea



Changes to  $K_S$  to change  $\omega_n$  of the sprung mass.

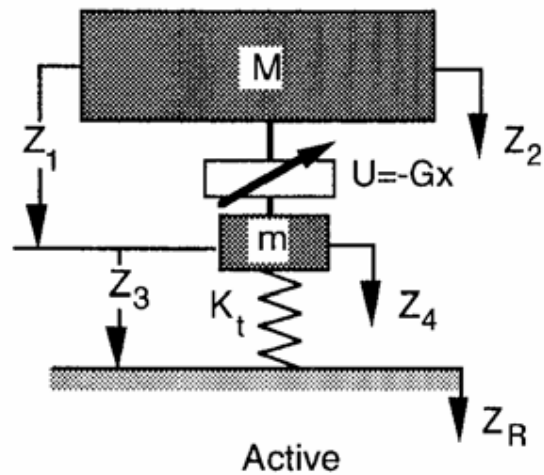
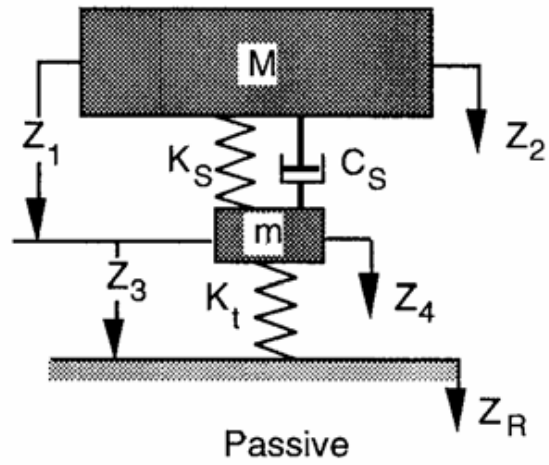
# Ride Response

- By changing damping also, the peak body response can be reduced.
- There are other consequences though for the higher frequencies whose transmission to the body becomes greater.

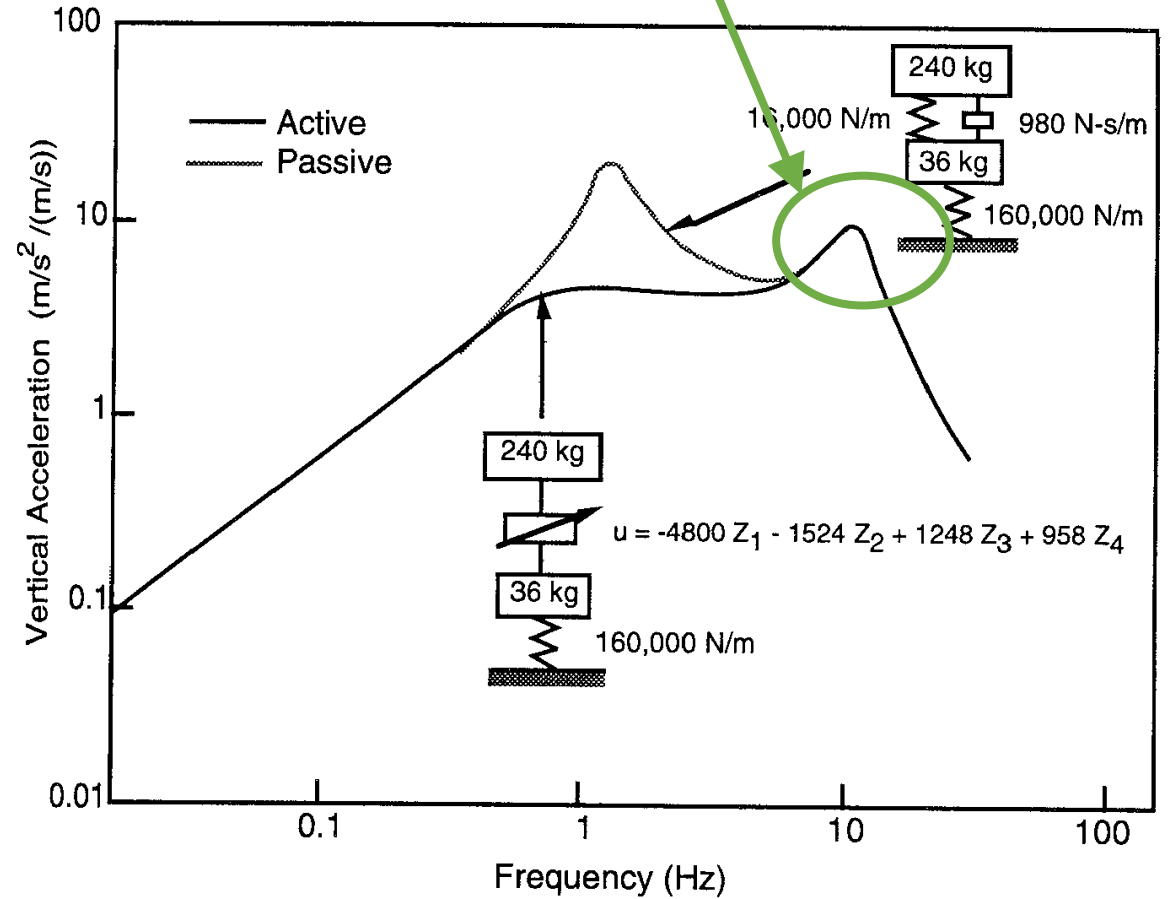


Effectively 'tied' together  
body and wheel.

# Active Suspension

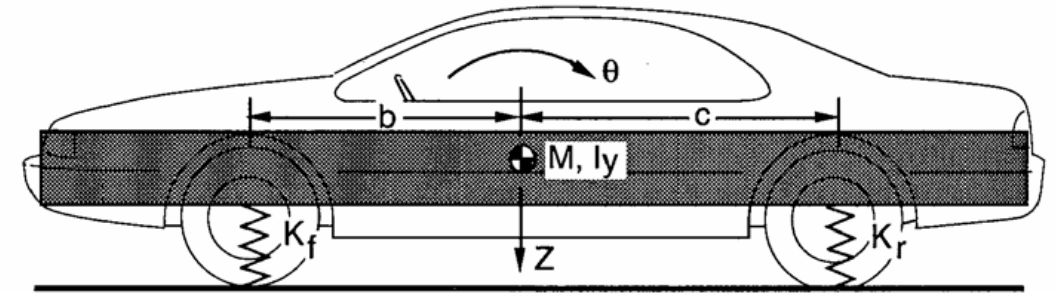


Less easy to manage wheel hop



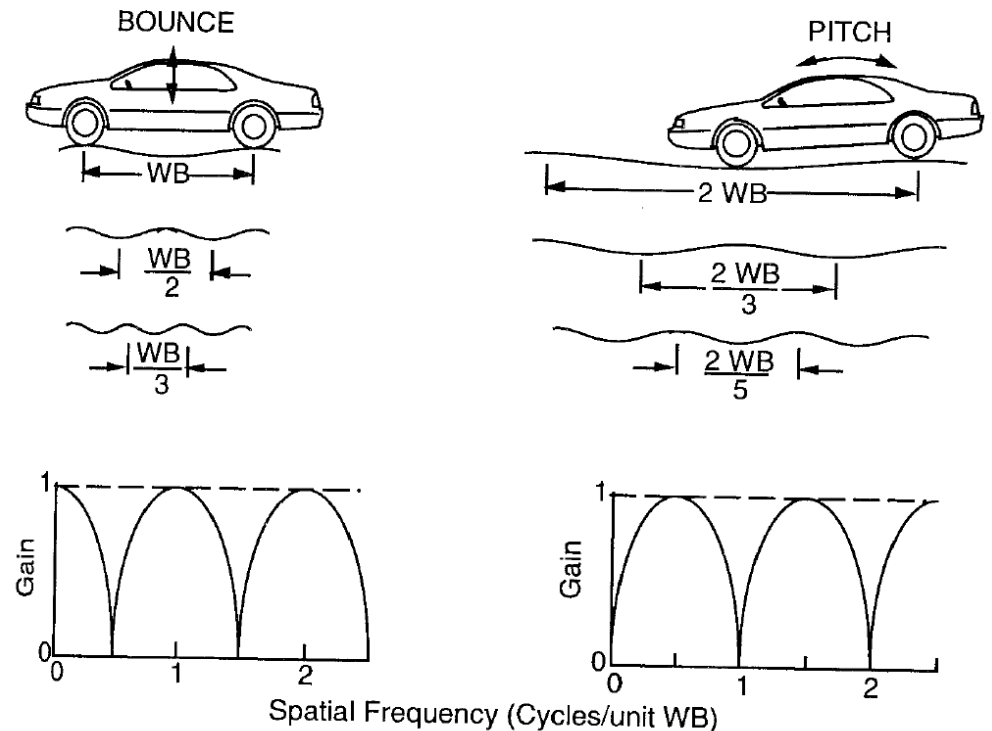
# Bounce and Pitch

- Quarter car model – good for body bounce analysis
- Half car model required for pitch and bounce analysis
- What you feel depends on where you are (centre vs one end or the other)
- Principle problem with pitch is the fore-aft motion it causes – nausea!



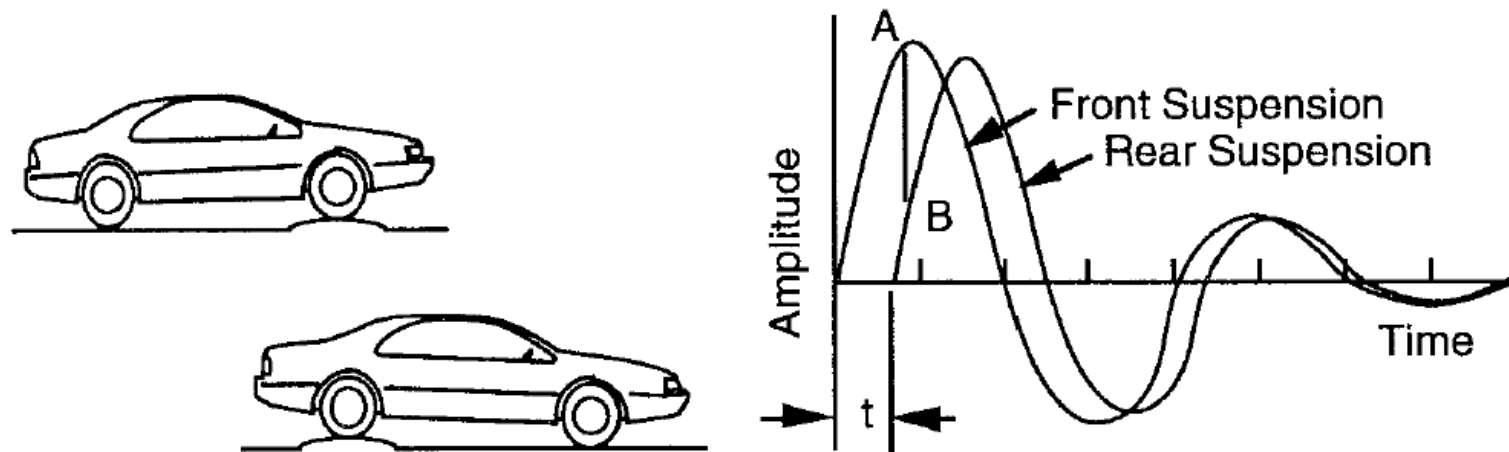
# Bounce and Pitch: Wheelbase Filtering

- Spacing of the front and rear suspensions can couple with road 'wavelength'.
- Very few roads are sinusoidal!





# Bounce and Pitch: Ride Rates

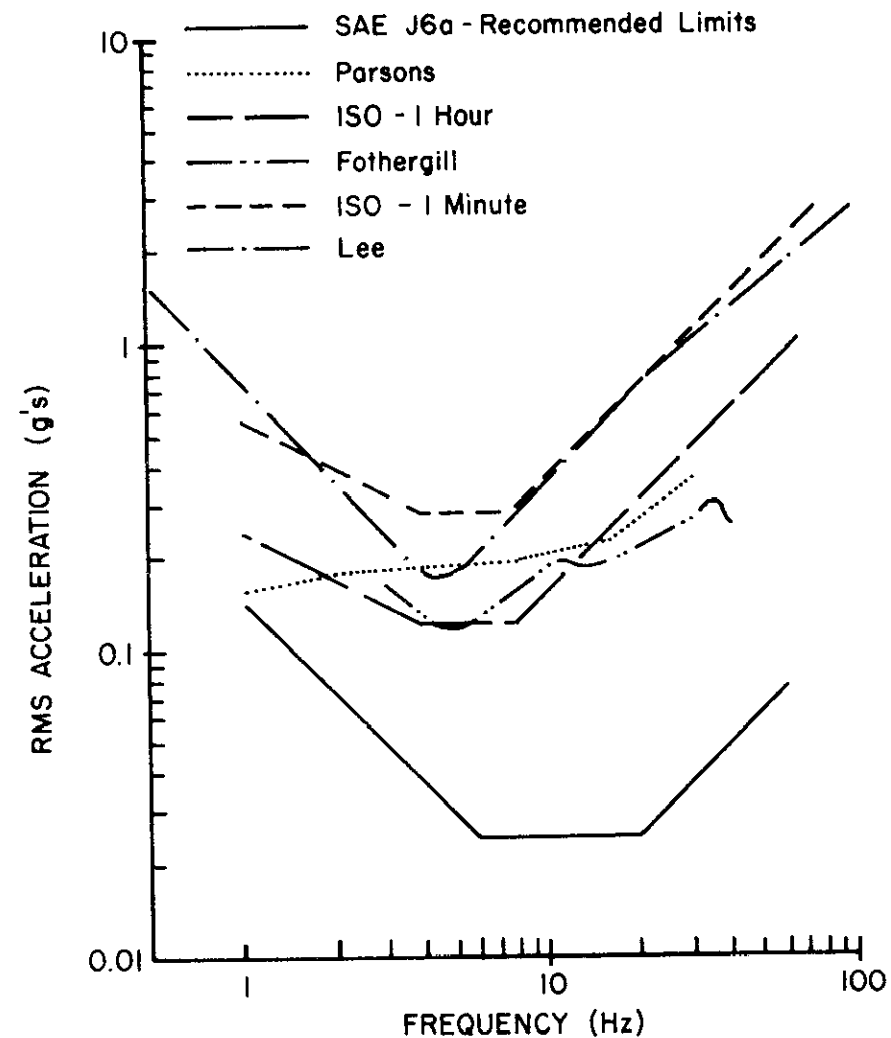


- By making front ride rate lower it is possible to reduce the discomfort of pitching.
- As you hit a bump this induces pitch but resolves to bounce as the rear end 'catches up' with the front.

# Human Perception

- We are interested in human perception
- Much like the vehicle the human body responds to different 'excitation' frequencies in different ways.

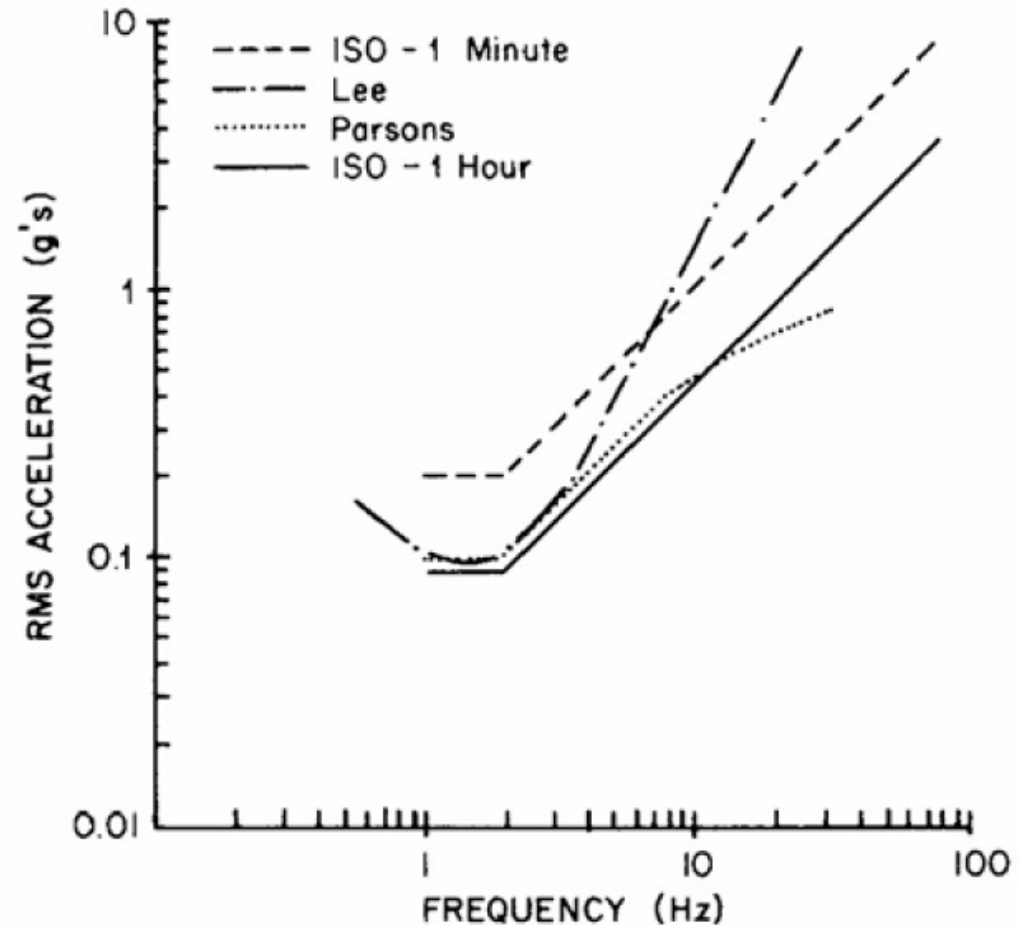
Ride discomfort (lines of equal tolerance) - vertical



# Human Perception

- Fore-aft vibration lines of 'equal comfort'
- Fore-aft tolerance no the same as vertical tolerance.

Ride discomfort (lines of equal tolerance) – fore-aft



# Conclusions

- Excitation input
- Quarter car model
- Ride response
  - Active suspension
- Human perception